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Modeling of laser-matter interaction: Linking theory and experiment

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Motivation



Irradiation of transparent materials with powerful laser beams



Two opposite research aims:

(1) To avoid damage: unwanted modification/cracking/defects in optics

(2) To increase energy coupling into a localized volume for achieving extreme states of matter; searching new polymorphs that possibly exhibit novel properties

<u>A large field in between</u>: how to gently modify material properties for laser direct writing of photonic structures which would enable light manipulations.

As a whole, the main aims of research are to learn how laser energy can be coupled in materials in the most efficient way; to predict and control the damage on the desired level, at a smallest volume; and/or to reach the highest possible stress level

Lasers in Material science

Many fascinating but still unclear phenomena

Trends

- State-of-art lasers with new radiation parameters
- Great variety of materials with very different properties
- Novel ("designed") materials
- Flexibility in irradiation conditions: vacuum/air/inert or reactive gases or liquids; mixed targets or simultaneous/alternating action of few laser beams on several targets

Q1. What is needed for developing successful applications

CONTROL over laser-induced processes in materials is of prime importance (INDUCED BY DIFFERENT LASERS IN DIFFERENT MATERIALS)

Processes in the pulsed laser excitation/ablation



How to understand which processes are behind a phenomenon observed?



Often, in science, the real answer is usually far from obvious. Discoveries are often done when scientists ask themselves "why did this happen?" or "why isn't this the result I expected?"

How to understand which processes are behind a phenomenon observed



Richard Phillips Feynman Observation > We try to guess





Experimental verification to check if our hypothesis/theory/modeling results are working

If the hypothesis contradicts to experiment, IT IS WRONG

IT IS NOT IMPORTANT:

How beautiful is our guess or hypothesis How clever is the author of hypothesis What is the name of the author

If the suggestion is not in agreement with experiment, it is false

Another problem, met not so rarely, is inaccurate modeling!

Mechanisms of nanosecond laser ablation

Laser light is absorbed by electrons

Electron-lattice thermalization time $\tau_{e-1} \sim 1-100 \text{ ps}$



Recoil pressure \rightarrow Hydrodynamic instabilities \rightarrow



Mechanisms of femtosecond laser ablation



Near-ablation-threshold fluences: Spallation



Thermal processes at laser fluences typical for material processing as a function of pulse duration

Laser-induced stress waves



M.V. Shugaev et al. Laser-Induced Thermal Processes: Heat Transfer, Generation of Stresses, Melting and Solidification, Vaporization, and Phase Explosion, In: *Handbook of Laser Micro- and Nano-Engineering*, K. Sugioka (ed.), Springer, Cham. (2021)

Thermal processes at laser fluences typical for material processing as a function of pulse duration: long pulse durations



Thermal processes at laser fluences typical for material processing as a function of pulse duration: ns pulse durations





Scales of laser-affected regions: - spot size ~10 μm – 1 mm; - depth ~10 nm - few μm (depending on laser focusing and absorption properties of irradiated material)

Density, thermal capacity, thermal conductivity, viscosity, mechanical properties (Young modulus, plastic yield, tensile strength), etc

Continuum

Modeling

Mesoscopic

Combines features of macroscopic and atomistic approaches



Stoneham et al. APA 69, S81 (1999)



Atomistic

CdTe



Interatomic potential of interaction

Thermal models

Pulse duration > τ_{e-1} • Heat transfer (one-temperature) model

$$C_l \frac{\partial T_l}{\partial t} = \frac{\partial}{\partial z} K_l \frac{\partial T_l}{\partial z} + \alpha (1 - R) I_0(t) \exp(-\alpha z)$$

Pulse duration $< \tau_{e-l}$

Two-temperature model
 Kaganov et al. Sov. Phys. JETP 4, 173 (1957)

$$\frac{\partial T_l}{\partial t} = \frac{T_e - T_l}{t_r}.$$

Anisimov et al. Sov. Phys. JETP 39, 375 (1974)

$$\begin{split} &C_e \frac{\partial T_e}{\partial t} = \frac{\partial}{\partial z} K_e \frac{\partial T_e}{\partial z} - g(T_e - T_l) + \alpha (1 - R) I_0(t) \exp(-\alpha z) , \\ &C_l \frac{\partial T_l}{\partial t} = \frac{\partial}{\partial z} K_l \frac{\partial T_l}{\partial z} + g(T_e - T_l) \end{split}$$

Continuum modeling

- Thermal models: based of one- and two-temperature heat flow equations
- Thermal models supplemented with the equations of thermoelasticity



- Thermal models supplemented with the Poisson equation: laser-induced material charging
- Hydrodynamic models



 Models based on Maxwell's equation (description of light propagation through transparent materials in the regimes of volumetric modification)

Free-electron generation and relaxation upon ultrashort laser pulse action



Example: Silicon excitation at 1030 nm



For silicon many years ago, we developed a model based on drift-diffusion approach which was largely based on van Driel model PRB 35, 8166 (1987) and partially on the paper by Sokolowski-Tinten and von der Linde, PRB 61, 2643 (2000). See, e.g., Bulgakova et al. PRB 69, 054102 (2004); APA 81, 345 (2005). All our simulations were performed for 800 nm wavelength.

Recently we applied this model for 1030 nm, our targeted wavelength. But the general aim was to verify the model and make it capable for description of ultrafast laser modification of semiconductors in a wide range of irradiation conditions.

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Main equations applied for silicon

Laser pulse
$$I(t) = (1 - R(t)) \frac{2F_0}{\tau_L} \sqrt{\frac{\ln 2}{\pi}} \exp\left(-4\ln 2\left(\frac{t}{\tau_L}\right)^2\right)$$
Attenuation in the bulk $\frac{\partial}{\partial x}I(x,t) = -(W_1n_a\hbar\omega + 2W_2n_a\hbar\omega I(x,t) + \alpha_{ab}(x,t))I(x,t)$
Rate equation $\frac{\partial n_{e,h}}{\partial t} = W_1I + W_2I^2 + \delta n_e - R_{Auger}$
Optical properties $\varepsilon^*(n_e) \cong 1 + (\varepsilon_g - 1)\left(1 - \frac{n_e}{n_0}\right) - \frac{n_e}{n_{cr}} \frac{1}{1 + i\frac{1}{\omega \tau}}$
Energy balance for laser energy source
$$\frac{\partial E_f}{\partial t} = \left((\hbar\omega - E_g)\frac{\sigma_1I}{\hbar\omega} + (2\hbar\omega - E_g)\frac{\sigma_2}{2}\frac{I^2}{\hbar\omega} - E_g\delta n_e\right)\frac{n_a}{n_a + n_i} + \alpha_{ab}(x,t)I(x,t) + E_gR_e$$

$$\frac{C_e}{\partial t}\frac{\partial T_e}{\partial t} = \frac{\partial}{\partial z}K_e\frac{\partial T_e}{\partial t} - g(T_e - T_l) + \frac{\partial E_f}{\partial t},$$
Temperatures as a measure of an average energy. In terms of enthalpy – the same results when taking care of algorithm accuracy.

when taking care

Parameters needed for simulations



$$\frac{\partial}{\partial x}I(x,t) = -(W_1 n_a \hbar \omega + W_2 n_a \hbar \omega I(x,t) + \alpha_{ab}(x,t))I(x,t)$$



Two-photon absorption as an averaged value for photoionization rate (e.g. threephoton direct absorption can be efficient but its rates are not known)

Melting threshold at 1030 nm

Two-photon absorption in our modeling 7 cm/GW

Thus, shortly:

In final model, we disregarded

- (1) Saturation of Auger recombination at high densities of free electrons
- (2) Increasing of e-ph coupling time at electron densities approaching and exceeding the critical plasma density
 All other provisions are similar to previous models developed for 800 nm

Bulgakova et al. PRB 69, 054102 (2004); APA 81, 345 (2005) Korfiatis et al. JPD 40, 6803 (2007); ASS 255, 7605 (2009) Rämer et al. JAP 116, 053508 (2014)



Next step:

Using **TDDFT** simulations to derive PI rates for 1030 nm and other wavelength

Time-dependent density functional theory



Deviation of negative charge from unexcited background upon laser excitation (arb.u.)



silicon atom

 hydrogen atom to stabilize silicon surface "Time-dependent density functional theory (TDDFT) can be viewed as an exact reformulation of time-dependent quantum mechanics, where the fundamental variable is no longer the many-body wave-function but the density." <u>http://www.tddft.org/</u>

TDDFT allows direct extraction of photoionization rates from first principles with no limitation inherent for Keldysh theory. MSCF project (Horizon 2020): T. J.-Y. Derrien; PRB 104, L241201 (2021)

Laser annealing of multilayer structures

V.A. Volodin et al. Opt. Las. Techn. 161, 109161 (2023)



Problem to solve:

You have two lasers, 2 ps at 1030 nm and 70 fs at 1500 nm You need to crystallize germanium to leave unaffected silicon for using in used in pi-n photodiodes or solar cells. You have to avoid intermixing of layers.

Q2. From what to start?

(1) materials properties

For modeling, it is necessary to collect the most reliable properties of materials involved

Parameter	a-Si	a-Ge
density, ρ, g/cm³	2.28 [Bäuerle]	5.15 [Goldschmidt]
heat capacity, c _p , J/(kg K))	800 [Bäuerle]	330 [Chen]
melting temperature, T _m , K	1420 [Bäuerle]	985 [Szyszko]
heat of fusion, ΔH_m , J/kg	1.25·10 ⁶ [Bäuerle]	3.5·10⁵[Szyszko]
band gap, E _g , eV	1.7 (direct) [Shoji]	~0.45 [Goh]
one-photon absorption coefficient, α , 1/cm	0.4 at 1030 nm [Boyuan] 10 ⁻² at 1500 nm [Shoji]	3·10⁴ at 1030 nm [Liu] 2.35·10³ at 1500 nm [Liu]
two-photon absorption coefficient, β , cm/GW	2 at 1030 nm [Bristow] [*] 0.08 1550 nm [Shoji]	taken as negligible for 1030 nm 12 cm/GW at 1050 nm [Garcia]*
reflection coefficient, R	0.4 at 1030 nm [Palik] 0.31 at 1500 [Palik]	~0.43 at 1030 nm [Liu] ~0.4 at 1500 nm [Liu]
Young's modulus, GPa	134 GPa [Kuschnereit]	126 [Zhan]
Poisson ratio, v	0.25 [Kuschnereit]	0.25 [Bharathan]
Linear thermal expansion coefficient, α_{I} , 1/K	1.10 ⁻⁶ [Takimoto]	1.7·10 ⁻⁵ (solid) [Persans] 0.9656·10 ⁻⁴ (liquid) [Rhim]
Rupture tensile strength, GPA	1.6 [Brookshire]	Unknown ¹

Q3. What next?

(2) Laser action \rightarrow photoionization (example of estimation)

$$\frac{\partial n_e}{\partial t} = \frac{(1-R)\alpha I(z,t)}{\hbar\omega} + \frac{(1-R)^2 \beta I^2(z,t)}{2\hbar\omega} + \delta(T_e)n_e - Cn_e^2 n_e^2 + \delta(T_e)n_e - Cn_e^2 n_e^2 + \delta(T_e)n_e - Cn_e^2 n_e^2 + \delta(T_e)n_e^2 + \delta(T_e$$

$$n_e \sim \frac{(1-R)\alpha I\tau}{\hbar\omega} + \frac{(1-R)^2 \beta I^2 \tau}{2\hbar\omega} = \frac{(1-R)\alpha F}{\hbar\omega} + \frac{(1-R)^2 \beta F^2}{2\hbar\omega\tau}$$

Results of estimations for 70-fs laser pulses at λ =1500 nm of the electron number densities generated in 1PA and 2PA processes, lattice temperature expected after electron-lattice thermalization, and the fraction of the molten phase *f*.

Fluence,		a-Si		a-Ge					
mJ/cm²	n _e , cm ⁻³ n _e , cm ⁻³ T, k (1PI) (2PI)	Τ, Κ	n _e , cm ⁻³ (1PI)	n _e , cm ⁻³ (2PI)	T+ΔΤ, Κ	T - f∆H _m , K	f		
40	<mark>2.16∙10¹⁵</mark>	<mark>3.4·10¹⁸</mark>	301	<mark>7.86∙10²⁰</mark>	<mark>3.86∙10²⁰</mark>	541	541	0	
55	<mark>2.96⋅10¹⁵</mark>	<mark>6.43∙10¹⁸</mark>	302	<mark>1.34⋅10²¹</mark>	<mark>7.3∙10²⁰</mark>	710	710	0	
70	<mark>3.77∙10¹⁵</mark>	<mark>1.04·10¹⁹</mark>	303.4	<mark>1.95·10²¹</mark>	<mark>1.18∙10²¹</mark>	896	896	0	
100	5.39.10 ¹⁵	<mark>2.12∙10¹⁹</mark>	306.7	<mark>3.5∙10²¹</mark>	<mark>2.4·10²¹</mark>	1370	985	0.36	
150	<mark>8.09∙10¹⁵</mark>	<mark>4.78∙10¹⁹</mark>	315	<mark>7.05·10²¹</mark>	<mark>5.4·10²¹</mark>	2457	1396	1	
190	<mark>1.02∙10¹⁶</mark>	<mark>7.64∙10¹⁹</mark>	325	<mark>1.08·10²²</mark>	<mark>8.7·10²¹</mark>	3604	2543	1	

Q4. What next?

(3) Temperature and molten fraction evaluation

 $c_p \rho \Delta T = (E_g + E_{\rm av}^e)$

 $f = c_p (T - T_m) / \Delta H_m,$

Results of estimations for 70-fs laser pulses at λ =1500 nm of the electron number densities generated in 1PA and 2PA processes, lattice temperature expected after electron-lattice thermalization, and the fraction of the molten phase *f*.

Fluence,		a-Si		a-Ge					
mJ/cm²	n _e , cm ⁻³ (1PI)	n _e , cm ⁻³ (2PI)	<mark>T, K</mark>	n _e , cm ⁻³ (1PI)	n _e , cm ⁻³ (2PI)	<mark>T+∆T, K</mark>	<mark>T - f∆H_m, K</mark>	f	
40	<mark>2.16⋅10¹⁵</mark>	<mark>3.4⋅10¹</mark> 8	<mark>301</mark>	<mark>7.86∙10²⁰</mark>	<mark>3.86⋅10²⁰</mark>	<mark>541</mark>	<mark>541</mark>	0	
55	<mark>2.96⋅10¹⁵</mark>	<mark>6.43∙10¹⁸</mark>	<mark>302</mark>	<mark>1.34·10²¹</mark>	<mark>7.3∙10²⁰</mark>	<mark>710</mark>	<mark>710</mark>	<mark>0</mark>	
70	<mark>3.77∙10¹⁵</mark>	<mark>1.04·10¹⁹</mark>	<mark>303.4</mark>	<mark>1.95∙10²¹</mark>	<mark>1.18∙10²¹</mark>	<mark>896</mark>	<mark>896</mark>	0	
100	<mark>5.39∙10¹⁵</mark>	<mark>2.12∙10¹</mark> 9	<u>306.7</u>	<mark>3.5∙10²¹</mark>	<mark>2.4·10²¹</mark>	<mark>1370</mark>	<mark>985</mark>	<mark>0.36</mark>	
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190	<mark>1.02⋅10¹⁶</mark>	<mark>7.64∙10¹</mark> 9	<mark>325</mark>	1.08·10 ²²	<mark>8.7·10²¹</mark>	<mark>3604</mark>	<mark>2543</mark>	1	

Crystallization of Ge layer; Si layers stay intact; no any signes of intermixing between Ge and Si layers that was requested for application



Fluence,		a-Si		a-Ge					
m5/cm-	n _e , cm ⁻³ (1PI)	n _e , cm ⁻³ (2PI)	<mark>Т, К</mark>	n _e , cm ⁻³ (1PI)	n _e , cm ⁻³ (2PI)	<mark>T+∆T, K</mark>	<mark>T - f∆H_m, K</mark>	f	
40	<mark>2.16⋅10¹⁵</mark>	<mark>3.4∙10¹</mark> 8	<mark>301</mark>	<mark>7.86·10²⁰</mark>	<mark>3.86∙10²⁰</mark>	<mark>541</mark>	<mark>541</mark>	0	
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70	<mark>3.77∙10¹⁵</mark>	1.04·10 ¹⁹	<mark>303.4</mark>	<mark>1.95∙10²¹</mark>	<mark>1.18⋅10²¹</mark>	<mark>896</mark>	<mark>896</mark>	0	
100	<mark>5.39∙10¹⁵</mark>	<mark>2.12⋅10¹⁹</mark>	<mark>306.7</mark>	<mark>3.5∙10²¹</mark>	2.4·10 ²¹	<mark>1370</mark>	<mark>985</mark>	<mark>0.36</mark>	
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Formation of GeSi alloy

(4) Stress-induced explosive crystallization

$$\sigma_r^{max} = \frac{E\alpha_l \Delta T}{2(1-\nu)},$$

The stresses in a-Ge nanolayers upon irradiation with 1500 nm wavelength are evaluated to increase from 0.34 GPa at 40 mJ/cm² to 0.97 GPa at 100 mJ/cm²

(5) *Can non-thermal melting promote a-Ge crystallization?* We note that, in fs irradiation regimes, the density of the ionized atoms in a-Ge approaches the criterium of ultrafast (non-thermal) melting (~10-15% of the valence electrons is pumped to the conduction band). Such excitation is almost immediately followed by lattice destabilization culminating innonthermal phase transitions (ultrafast melting) on a sub-ps time scale. Although ultrafast melting in *amorphous* semiconductors looks to be unobservable, lattice atoms become mobile and can form crystallites. For low-bandgap semiconductors as a-Ge, from the energy balance one can expect a situation when ultrafast melting is not followed by thermal melting.

Fluence,		a-Si		a-Ge					
mJ/cm²	n _e , cm ⁻³ (1PI)	n _e , cm ⁻³ (2PI)	T, K	n _e , cm ⁻³ (1PI)	n _e , cm ⁻³ (2PI)	<mark>T+∆T, K</mark>	<mark>T - f∆H_m, K</mark>	f	
40	<mark>2.16⋅10¹⁵</mark>	<mark>3.4∙10¹⁸</mark>	<mark>301</mark>	<mark>7.86∙10²⁰</mark>	<mark>3.86∙10²⁰</mark>	<mark>541</mark>	<mark>541</mark>	0	
55	<mark>2.96∙10¹⁵</mark>	<mark>6.43∙10¹⁸</mark>	<mark>302</mark>	1.34·10 ²¹	<mark>7.3∙10²⁰</mark>	<mark>710</mark>	<mark>710</mark>	0	
70	<mark>3.77∙10¹⁵</mark>	1.04·10 ¹⁹	<mark>303.4</mark>	<mark>1.95⋅10²¹</mark>	<mark>1.18⋅10²¹</mark>	<mark>896</mark>	<mark>896</mark>	0	
100	<mark>5.39∙10¹⁵</mark>	<mark>2.12⋅10¹⁹</mark>	<mark>306.7</mark>	<mark>3.5∙10²¹</mark>	2.4·10 ²¹	<mark>1370</mark>	<mark>985</mark>	<mark>0.36</mark>	
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If the hypothesis contradicts to experiment, IT IS WRONG

as a-Ge, from the energy balance one can expect a situation when ultrafast melting is not followed by thermal melting.

Fluence,		a-Si		a-Ge					
mJ/cm²	n _e , cm ⁻³ (1PI)	n _e , cm ⁻³ (2PI)	<mark>Т, К</mark>	n _e , cm ⁻³ (1PI)	n _e , cm⁻³ (2PI)	<mark>Τ+ΔΤ, Κ</mark>	<mark>T - f∆H_m, K</mark>	f	
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Tasuku Honjo, an immunology and genomic medicine professor at Kyoto University (2018 Nobel Prize in Physiology or Medicine and is best known for his identification of programmed cell death protein), said his advice for people who want to pursue a career in scientific research what he called the "six Cs":

curiosity, courage, challenges, continuation, concentration and confidence.











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